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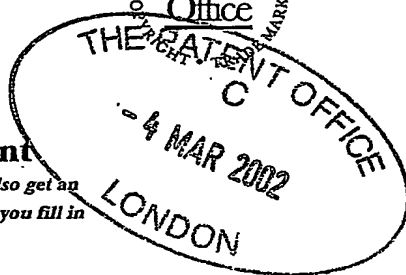
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2. Patent application number (The F)	0205000.3		
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Patents ADP number (<i>if you know it</i>)			
If the applicant is a corporate body, give the country/state of its incorporation	United Kingdom		
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4. Title of the invention	UNSUPERVISED DATA SEGMENTATION		
5. Name of your agent (<i>if you have one</i>)	J.A. KEMP & CO.		
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UNSUPERVISED DATA SEGMENTATION

The present invention relates to a method and apparatus for unsupervised data segmentation which is suitable for assigning multi-dimensional data points of a data set amongst a plurality of classes. The invention is particularly applicable to automated image segmentation, for instance in the field of medical imaging, thus allowing different parts of imaged objects to be recognised and demarcated automatically.

In the field of automated data processing it is useful to be able to recognise automatically different groups of data points within the data set. This is known as segmentation and it involves assigning the data points in the data set to different groups or classes.

An example of a field in which segmentation is useful is the field of image processing. A typical imaged scene contains one or more objects and background, and it would be useful to be able to recognise reliably and automatically the different parts of the scene. Typically this may be done by segmenting the image on the basis of the different intensities or colours appearing in the image. Image segmentation is applicable in a wide variety of imaging applications such as security monitoring, photo interpretation, examination of industrial parts or assemblies, and medical imaging. In medical imaging, for instance, it is useful to be able to distinguish different types of tissue or organs or to distinguish abnormalities such as an aneurysm or tumour from normal tissue. Currently, particularly in medical imaging, segmentation involves considerable input from a clinician in an interactive method.

For example, there have been proposals for methods of demarcating an aneurysm in an image of vasculature by first identifying the aneurysm neck, then labelling all pixels on one side of the neck as forming the aneurysm, while pixels on the other side are identified as part of the adjoining vessel. Such techniques are described in R. van der Weide, K. Zuiderveld, W. Mali and M. Viergever, "CTA-based angle selection for diagnostic and interventional angiography of saccular intracranial aneurysms", IEEE Transactions on Medical Imaging, Vol. 17, No. 5,

pp831-341, 1998 and D. Wilson, D. Royston, J. Noble and J. Byrne, "Determining X-ray projections for coil treatments of intracranial aneurysms", IEEE Transactions on Medical Imaging, Vol. 18, No. 10, pp973-980, 1999. However, these techniques also rely on manual intervention for starting the segmentation.

5 Techniques of segmentation using region-splitting or region growing are well known, see for example: Rolf Adams and Leanne Bischof, "Seeded Region Growing", IEEE Transactions on Pattern Analysis and Machine Intelligence, Vol.

16, No. 6, pp641-647, Jun, 1994. However, these techniques require that the number of regions into which the data set is to be segmented is known in advance. Thus the
10 techniques are not generally applicable to fully automatic methods.

Segmentation techniques in which there is no initial assumption of the number of classes found in the data set are referred to as "unsupervised" segmentation techniques. An unsupervised segmentation algorithm has been proposed in Charles Kervrann and Fabrice Heitz, "A Markov Random Field model-
15 based approach to unsupervised texture segmentation using local and global spatial statistics", Technical Report No. 2062, INRIA, Oct, 1993. This utilises an augmented Markov Random Field, where an extra class label is defined for new regions, and a parameter is pre-set to define the probability assigned to this extra
20 state. Any points in the data set which are modelled sufficiently badly (assigned a low probability by the existing classes) will be assigned to this new class. At each iteration of the algorithm, connected components of such points are collated into new classes.

However, typical problems with unsupervised techniques are under-segmentation (in which data points are added to inappropriate classes) and over-
25 segmentation (in which the data is divided into too many classes).

One aspect of the present invention provides an unsupervised segmentation method which is generally applicable to multi-dimensional data sets. Thus, it allows for completely automatic segmentation of the data points into a plurality of classes, without any prior knowledge of the number of classes involved.

30 In more detail this aspect of the invention provides an unsupervised

segmentation method for assigning multi-dimensional data points of a selected data set amongst a plurality of classes, the method comprising the steps of:

- (a) defining an initial class encompassing all data points of the selected data set;
- 5 (b) defining a second class by selecting a data point and assigning it to the second class together with data points within a first predetermined neighbourhood of the selected data point;
- (c) testing each data point lying within a second predetermined neighbourhood of data points in the second class by calculating the probability that each said data point belongs to the first class and the
10 probability that it belongs to the second class, and assigning it to the second class if the probability that it belongs to the second class is higher;
- (d) said probability calculations being adapted during said method in dependence upon the assignment of the points to the classes.

- 15 The probability calculations may comprise the steps of determining a probability distribution of a property of the data points in the initial class and determining a probability distribution of said property of the data points in the second class, and comparing the data point under test with the two probability distributions. The probability calculations may also comprise the step of multiplying
20 the probability derived from the probability distribution with an *a priori* probability derived, for example, from the proportion of points in the neighbourhood in the various classes.

- The calculation of probability may be adapted as the method proceeds by recalculating the probability distributions as data points are assigned to the classes.
- 25 The distributions will alter as the number of data points in the data points varies. This adaptation may take place every time a point is reassigned, or after a few points have been reassigned.

- The classes continue to grow as more data points are assigned to them. Preferably the method continues until no more data points are added to the class, at
30 which point another class may be defined and then grown by repeating the method

steps.

The selection of the data point for initiating a class may be random, or it may be optimised, for example by ordering the remaining points based on the probability distribution.

- 5 Preferably classes are discarded (or "culled") if they fail to grow, i.e. if they fail to have data points assigned to them when all necessary points have been tested. This is particularly useful in avoiding over-segmentation of the data set.
-

Segmentation is concluded when all of the classes formed in turn on the basis of the data points remaining in the initial class have been discarded.

- 10 A predetermined neighbourhood of a data point d is an open set that contains at least the data point itself. One example is the open ball of radius r which contains all data points within a distance r of the data point d , though other shapes are possible and may be appropriate for different situations. In extreme cases, a neighbourhood may contain only the data point itself, or may contain the entire data set. The first
- 15 and second predetermined neighbourhoods may be defined only on the spatial position of the data points, for instance in the application of the technique to an image where the aim is to segment the image into the different parts of the imaged object. However, in other data sets the neighbourhoods may be defined in a parameter space containing the data points.

- 20 Where the technique is applied to image segmentation, the data points may comprise a descriptor of at least a part of an object in the image and the spatial coordinates of that part. The descriptor may be representative of the shape, size, intensity (brightness), colour or any other detected property, of that part of the object.

- Rather than taking the data points from the image itself, they may be taken
- 25 from a spatial model fitted to the image, such as a 3-D mesh fitted to the image or its segmentation. This is particularly useful where the descriptor is a descriptor of the shape of the object.

 The image may be a volumetric image or a non-invasive image, and for example may be an image in the medical field or industrial field (e.g. a part x-ray).

- 30 Another aspect of the invention provides a method of demarcating different

parts of a structure in a representation of the structure, comprising the steps of calculating for each of a plurality of data points in the representation at least one shape descriptor of the structure at that point, and segmenting the representation on the basis of said at least one shape descriptor.

5 The representation may be an image of the structure, or may be a 3-D model of the structure (which could be derived by various imaging modalities). The results may be displayed in the form of a visual representation of the structure, with the parts distinguished, for instance by being shown in different colours.

10 The descriptor may comprise values representing cross-sectional size or shape of the structure at that point. The values may be lateral dimensions of the structure at that point.

 The descriptors may be used to segment the representation automatically, for example using an unsupervised segmentation method such as the method in accordance with the first aspect of the invention.

15 The image may be a volumetric image or a non-invasive image, and for example may be an image in the medical field or industrial field (e.g. a part x-ray). In the medical field the method may be used to demarcate an aneurysm from vasculature, or to demarcate other protrusions.

20 The invention extends to a computer program comprising program code means for executing the methods on a suitably programmed computer. Further, the invention extends to a system and apparatus for processing and displaying data utilising the methods.

 The invention will be further described by way of example, with reference to the accompanying drawings in which:-

25 Figure 1 illustrates schematically an imaging system in accordance with one embodiment of the invention;

 Figure 2 is a flow diagram of one embodiment of the invention;

 Figures 3A and 3B show respectively a 3-D model of an aneurysm and adjoining vessels and a mesh computed for the 3-D model;

30 Figure 4 illustrates schematically a blood vessel and aneurysm indicating the

shape descriptors used in an embodiment of the present invention;

Figure 5 illustrates the concepts of data point classes and regions used in one embodiment of the present invention;

Figure 6 illustrates a synthetic data set containing three groups of data points;

5 Figure 7 illustrates an initial probability distribution for the data set of Figure 6;

Figures 8A and 8B illustrate respectively a newly seeded class in the data set of Figure 6 and the initial probability distribution for that class;

Figure 9 illustrates the classification after the class of Figure 8 has converged;

10 Figure 10 illustrates the classification after a further class has converged;

Figures 11A, B and C illustrate probability densities for the classes in Figure 10;

Figures 12 A and B illustrate the seeding of a further class and its initial probability distribution;

15 Figure 13 illustrates the final segmentation of the data set of Figure 6 achieved with one embodiment of the present invention, and

Figures 14 and 15 illustrate the results of applying the image segmentation method of an embodiment of the invention to medical images.

An embodiment of the invention applied to the shape based segmentation of
20 an image of vasculature including an aneurysm and to the intensity based segmentation of a synthetic image will be described below. However, it will be appreciated that the segmentation technique is applicable to the segmentation of general data sets having data points in n -dimensions, where each data point has m numeric values. Thus it may be applied, for example, to intensity-based
25 segmentation, for instance of ultrasound, MRI, CTA, 3-D angiography or colour/power Doppler data sets, to the segmentation of PC-MRA data where a scan provides information on the speed (intensity) and an estimated flow direction, and to unsupervised texture segmentation as well as object segmentation of parts based on geometry.

30 Figure 1 illustrates schematically the apparatus used in one embodiment of

the invention which comprises an image acquisition device 1, a data processor 3 and an image display 5. The operation of the apparatus is illustrated schematically by the flow diagram of Figure 2 and involves the general steps acquiring the image in step s1, segmenting the image in step s3 and displaying the segmented image in step s4.

- 5 In this embodiment of the invention the segmentation is carried out on a three dimensional model of the imaged object (in the example below of vasculature) calculated in step s2 by standard techniques such as A.C.S Chung and J.A. Noble, "Fusing magnitude and phase information for vascular segmentation in phase contrast MR angiograms", Proceedings Medical Image Computing and Computer
10 Assisted Intervention. (MICCAI), pp. 166-175, 2000 and D.L. Wilson and J.A. Noble, "An Adaptive Segmentation Algorithm for Time-of-Flight MRA Data", IEEE Transactions on Medical Imaging, Vol. 18, No. 10, pp 938-945, Oct, 1999, IEEE.

A brain aneurysm is a localised persistent dilation of the wall of a blood vessel. Visually, it appears that part of the vessel has ballooned out. When the
15 ballooning vessel pops, it will often result in the death of the patient. There are several possible treatments for an aneurysm including surgery (clipping) or filling the aneurysm with coils. The type of treatment is dependent upon factors such as aneurysm volume, neck size and the location of the aneurysm in the brain.

- It is usual to image the aneurysm and related blood vessels using a 3-D
20 imaging modality such as MRA, CTA or 3-D Angiography. Such scans may be segmented to extract blood vessels and aneurysm from tissue and air. The segmented data can then be used to produce a 3-D model of the vessels and aneurysm. Given such a 3-D model, it is useful to demarcate the aneurysm, identifying where it connects to the major vessel. This allows the estimation of aneurysm volume and
25 neck size and other geometry-related parameters, and hence aids the clinician to choose the appropriate treatment for a particular patient and possibly to use the information in the actual treatment (eg to select views of the aneurysm). In this embodiment the aneurysm is demarcated by first computing a triangular mesh over the 3-D model. Such a mesh can be computed using an established mesh method
30 such as the marching cubes algorithm. An example of a 3-D model showing an

aneurysm and the adjoining vessels, and its associated mesh is illustrated in Figures 3A and B. The aneurysm is the large ballooning section near the centre of the image.

The segmentation will be carried out in this embodiment using two values which form a shape descriptor, i.e. a description of the shape of the vasculature at that point. At each vertex in the triangular mesh, a local description of the vessel shape is computed, as shown in Figure 4. Taking the unit surface normal n_i to the mesh at a particular vertex v_i , a ray is extended from v_i into the vessel and the distance to the opposite side of the vessel is measured. Halving this value gives an estimate of the vessel radius r_i at v_i . This estimate of vessel radius is the first of two descriptors that are computed.

Using r_i , the point p_i is defined as an estimate of the vessel centre, defined as $p_i = v_i + r_i n_i$.

The two directions of principal curvature on the mesh, that is the directions in which the curvature of the mesh at v_i are a maximum and minimum can then be estimated. Denoting these directions as c_{max} and c_{min} , where the absolute value of c_{max} is larger than the absolute value of c_{min} , a vector from p_i in the directions of c_{max} and $-c_{max}$ is extended, measuring the distance in each direction to the vessel surface. Adding these two distances together gives an estimate of the vessel diameter d_i in a direction perpendicular to n_i .

The two values (r_i, d_i) form the shape descriptor which characterises the vessel at the point v_i and are computed for every vertex in the mesh

The task is now to segment the data set to demarcate the aneurysm, i.e. to group together points that lie on the aneurysm and to distinguish these from points on the adjoining vessels. This will allow the aneurysm to be demarcated. Points lying along the single blood vessel will have similar values for (r_i, d_i) . At the neck of the aneurysm, these values will change rapidly. Passing over the neck and onto the aneurysm itself, there will be a similarity in the values on the aneurysm.

Segmentation is achieved in this embodiment by using a region splitting algorithm. The algorithm separates the points on the triangular mesh into regions (sub-parts) that are similar. Each vessel should be identified as a sub-part, while the

aneurysm will form a different sub-part.

Firstly, to illustrate the concepts used in the segmentation method it will be helpful to consider the simple set of points illustrated in Figure 5. Suppose the task is to classify data point d_0 . It is assumed that it must be in the same class as one of the other five data points that lie within the dotted circular neighbourhood, i.e. within a distance $r_{classify}$ of the data point under consideration. Of these, as indicated in Figure 5, d_1 and d_2 belong to class C_1 ; d_3 and d_4 belong to class C_2 ; and d_5 belongs to class C_3 . The point d_0 will be classified depending upon some property which it holds in common with the data points in one of the other classes. This property may, for example, be its intensity or colour if the points are pixels in an image, or a shape descriptor such as that described above in connection with the task of aneurysm demarcation, and can be a scalar or n-vector quantity. The approach in this embodiment is to calculate the probabilities in turn that the point d_0 is in each of the classes C_1 , C_2 or C_3 , and then to assign it to the class for which the probability is the highest. In this embodiment the probability will be the product of two terms. The first is a probability that is independent of the property of interest of d_0 . The second is a probability based on the value of the property (for example intensity or shape descriptor) of the point and a comparison with the distribution of such values in each of the three classes.

Taking the first of those probabilities, there are several ways of calculating this probability. One way is to set it as being directly proportional to the number of data points of each class within the radius $r_{classify}$. For example, referring to Fig. 5, this probability term as regards class C_1 would be $2/5$ because 2 of the 5 points within the distance $r_{classify}$ are points of class C_1 . There are other possibilities, such as setting the probability in accordance with the Euclidean distance in real or parameter space between the various points. This term, which does not depend on the value of the property of interest at the data point, is known as the "*a priori*" probability.

The second term, based on the value of the property of interest of point d_0 (such as intensity or shape descriptor) is, in this embodiment, obtained by comparing the value of the property for d_0 to the distribution of such values in the three classes

C_1, C_2, C_3 . This will be described below with reference to a specific intensity-based example illustrated in Figure 6. Figure 6 illustrates a data set which consists of intensity values. The aim is to segment this image automatically into the three regions or classes which are clearly visible. The first step is to assign all data points (in this case pixels) to a single initial class C_0 . Then the probability distribution (in this case of intensity on a gray scale) over the class C_0 is calculated. In this case it is calculated by computing a histogram of the values of intensity (i.e. binning the

intensity values, counting the number of values within each bin, and normalising the total count to 1). The histogram is then smoothed using Parzen windows by convolving the values in the histogram using a kernel function. The kernel function used in this embodiment is the Gaussian function, although others may be used. This smoothing function is adaptive as will be explained below. The result is the initial probability distribution as illustrated in Figure 7. Incidentally, in Figure 7 three peaks corresponding to the three classes of Figure 6 can be seen.

The next step is to start or "seed" a new class. This is achieved by choosing a data point, defining a neighbourhood of radius r_{seed} around it, and assigning all points within the neighbourhood to the new class C_1 . This is illustrated in Figure 8A. In some embodiments the point may be chosen randomly, although in other embodiments the points in the data set may be ordered for selection, for instance in accordance with how badly they are modelled by the remaining class. It can be seen that the new class C_1 happens to be in the bottom left-hand area of the image. Then the probability distribution of intensity values is calculated for the class C_1 in just the same way as the probability distribution above (namely by forming a histogram and then smoothing it). This probability distribution is illustrated in Figure 8B.

It was mentioned above that the smoothing is adaptive. In this embodiment this is achieved by making the variance of the Gaussian kernel function dependent upon the number of data points in the class. This greatly affects the probability distribution produced. When the histogram comprises only a small number of values, it is appropriate to use a large variance. This results in heavy smoothing. If the histogram consists of a large number of values, it is more likely that the

probability distribution accurately reflects the underlying distribution, and so a small variance is appropriate, resulting in less smoothing. The variance may be defined as a function of the number of data points in a class, such that as the number of data points in the class increases, the variance decreases. In this example, the variance is
5 inversely proportional to the square of an affine function of the size of the class. Other functions are possible. For example, the variance may be inversely proportional to the natural logarithm of the number of data points in the class.

Note that functions other than a Gaussian can be used as the kernel function for the Parzen window estimate of the probability distribution. In this case, some
10 property of the kernel function comparable to the Gaussian's variance will be adjusted as a class grows or shrinks.

The next step is to test data points near the class C_i to check whether they can be assigned to class C_i not. In this embodiment all points d_j are tested which lie within a radius $r_{classify}$ of any point in the class C_i . The testing involves selecting a
15 point d_j and computing the probabilities that this point belongs to class C_0 or C_i . For each class, this involves computing two values, which are multiplied together to compute the probability.

The first value is the *a priori* probability that d_j belongs to each class. As mentioned above this probability is independent of the value of the property of
20 interest. In this example it is taken as the proportion of points within a radius r_{seed} of d_j that are in the relevant class, as explained in relation to Figure 5.

The second value is computed by comparing the value of the property of interest (intensity or shape descriptor etc) with the probability distributions computed for the class. For classes C_0 and C_i these probability distributions are shown in
25 Figure 7 and 8B. Thus, for example, if the point d_j has an intensity corresponding to the value 20 on the horizontal axis of the distribution, the value for class C_0 can be read off as 0.010 whereas the value for class C_i can be read off as about 0.027. These values are multiplied with the *a priori* probabilities to give the probability that data point d_j belongs to either class C_0 or C_i . In the example of the two values that
30 we have quoted, where d_j has an intensity of 20, if the *a priori* probabilities are of a

similar magnitude, then class C_1 will have a higher probability and the data point will be assigned to class C_1 .

Thus the class C_1 grows with each point that is assigned to it. The testing is repeated recursively, choosing all points within a radius $r_{classify}$ of each point added to class C_1 and testing whether they should be reclassified to class C_1 . It should be noted that only points which are currently in class C_0 are considered (in other words reclassified points are not subsequently reconsidered). It is important to note, though, that each time a point is reassigned, the probability distributions for the two classes are recalculated with a new variance for the Gaussian kernel set in accordance with the change in the number of points. Where there are a large number of data points such that the probability distribution does not vary much as a single point is reassigned, the recalculation of the probability distribution need not occur every time a point is reassigned, but after a preset number of points have been reassigned. This means that the probability distribution varies adaptively as the classification process proceeds.

The variance used, therefore, when computing the probability that a point under test belongs to the initial class C_0 will increase as points are removed from the class, and the variance used to compute the probability that the point belongs to class C_1 will decrease as that class grows. In this way, C_1 will improve its model of the distribution of numeric values for the property of interest in the class, and this distribution will be removed gradually from the three distributions that together formed the distribution for class C_0 illustrated in Figure 7.

The process of testing points for addition to class C_1 is continued until no new points within a radius $r_{classify}$ of the existing points in the class are added. This is the situation indicated in Figure 9. If viewed graphically, the class C_1 appears to "flood-fill" out to the borders of the class as shown in Figure 9.

Then the process is repeated by seeding a new class C_2 on a point in class C_0 and growing that class. Whilst growing the class C_2 , when testing whether to reassign some point d_j from class C_0 to class C_2 , it may be found that points from class C_1 also lie within a neighbourhood of radius $r_{classify}$ of d_j . In this case, it is tested

whether to assign data point d_j to class C_0 , C_1 or C_2 .

After this second class C_2 has converged, the data will be classified into C_0 , C_1 and C_2 as shown in Figure 10. Figure 11 shows the probability distributions for the three classes.

5 Because this is an unsupervised algorithm, the process does not, of course, "know" that there are no more classes of points. Therefore the process will continue by seeding a new class C_3 as shown in Figure 12A. The initial probability distribution for class C_3 is shown in Figure 12B. However, this class will, in fact, not grow in the way that C_1 and C_2 did. The algorithm is designed to discard classes
10 which do not grow (by reclassifying their points back to class C_0). The reason that class C_3 does not grow will be explained. First, because C_3 contains fewer points than C_0 , the probability distribution is generated by convolving with a Gaussian kernel function with a large variance. Thus it is more smoothed than the probability distribution for the remaining points in C_0 . This results in lower probabilities being
15 read off for values from the underlying distribution. It will be seen that in Figure 12B the maximum probability is 0.045, while the maximum for the remaining class C_0 is 0.06 as shown in Figure 11A. Thus as class C_3 attempts to grow, by testing data points, most points will not be re-classified from C_0 to C_3 , but will remain instead in C_0 . If the class does not grow sufficiently it will be "culled". The growth is tested
20 against a threshold. In this example if, at convergence, a class is less than three times as large as when it was seeded it is culled. Other criteria, for example based on the rate of growth, are possible. In this way the algorithm does not introduce an excessive number of classes to the segmentation.

In practice the algorithm continues to attempt to seed new classes on each of
25 the points left in C_0 , but each new class will be culled. The final segmentation is shown in Figure 13. It can be seen that the segmentation is fairly accurate.

It should be noted that the algorithm can be applied again within each of the classes C_0 , C_1 , C_2 to check for segmentation within those classes. Thus each class is taken in turn, all its data points regarded as an initial class and a new class seeded
30 within it, the method then proceeding as before.

The data set need not comprise all data points available (e.g. all pixels in the image or all points in the model). A subset of the data points may be selected to optimise the segmentation (e.g. by excluding obvious outliers). In addition, not all data points in a class may be used in the computation of the probability distribution.

- 5 A subset of the data points may be selected (e.g. by excluding outliers according to some statistical test).

The algorithm therefore involves segmenting a data set by initially assigning all points to a single class and then randomly seeding and growing new classes. The probability distributions in the classes are adaptive and this, together with the culling
10 of classes which do not grow, means that over-segmentation is avoided.

In applying the algorithm to the problem of demarcation of an aneurysm, instead of intensity values, the two-dimensional shape descriptor is used. Thus, referring to Figure 3, the 3-D model of the aneurysm and blood vessels is calculated from an image of the vasculature and a triangular mesh is defined over the model. At
15 each point on the mesh the two-dimensional data points (r_i , d_i) are computed which describe the shape of the vessel or aneurysm at that point. The algorithm is then applied by initially assigning all points to the same region, and then seeding a new region somewhere on the mesh. The method attempts to grow this new region. If it does not grow, it is culled. At completion, the mesh is separated into the appropriate
20 regions, with the aneurysm separated from its adjoining vessels on the basis of its shape descriptor.

Figures 14 and 15 show the application of an embodiment of the invention to two clinical data sets. The results for two patients with aneurysms are shown and in each case the three views of the 3-D brain model are shown on the left, and the
25 segmented results on the right. In each case the aneurysm present is successfully identified.

The method can, of course, be applied also to intensity-based segmentation, such as the segmentation of B-mode ultrasound follicle images where it has successfully demarcated regions indicating follicles. The method is also applicable
30 to the segmentation of MRI, CTA, 3-D angiography and colour/power Doppler sets

where blood can be distinguished from other tissue type by its intensity.

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CLAIMS

1. An unsupervised segmentation method for assigning multi-dimensional data points of a selected data set amongst a plurality of classes, the method comprising the

5 steps of:

(a) defining an initial class encompassing all data points of the selected data set;

10 (b) defining a second class by selecting a data point and assigning it to the second class together with data points within a first predetermined neighbourhood of the selected data point;

(c) testing each data point lying within a second predetermined neighbourhood of data points in the second class by calculating the probability that each said data point belongs to the first class and the probability that it belongs to the second class, and assigning it to the second
15 class if the probability that it belongs to the second class is higher; and
(d) said probability calculations being adapted during said method in dependence upon the assignment of the points to the classes.

2. A method according to claim 1 wherein the probability calculations comprise the
20 steps of determining a probability distribution of a property of the data points in the initial class and determining a probability distribution of said property of the data points in the second class and comparing the data point under test with said probability distributions.

25 3. A method according to claim 1 or 2 wherein said calculation is adapted by recalculating said probability distributions as data points are assigned to classes.

4. A method according to claim 3 wherein said probability distributions are recalculated on the basis of the number of data points in each class.

5. A method according to claim 4 wherein said probability distributions are recalculated after each assignment of a data point.

6. A method according to any one of the preceding claims wherein steps (b), (c) and
5 (d) are repeated iteratively testing in step (c) data points lying within the second predetermined neighbourhood of data points assigned to the second class.

7. A method according to claim 6 wherein steps (b) to (d) are repeated iteratively until no more data points are added to the second class.

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8. A method according to any one of the preceding claims further comprising the step of defining a third class by selecting a data point from the initial class and assigning it to the third class together with data points within the first predetermined neighbourhood of the selected data point, and repeating the method iteratively with
15 respect to the third class.

9. A method according to any one of the preceding claims further comprising the step of discarding any class which fails to have sufficient data points assigned to it in step (c) according to a predetermined criterion, by reassigning its data points to the
20 initial class, when all data points within said predetermined neighbourhood have been tested.

10. A method according to claim 9 further comprising the step of concluding the segmentation when all classes formed in turn on the basis of selecting each of the
25 data points remaining in the initial class have been discarded.

11. A method according to any one of the preceding claims wherein said first and second predetermined neighbourhoods are open spheres centred on the data point and having a predetermined radius.

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12. A method according to any one of the preceding claims wherein said first and second predetermined neighbourhoods are defined on a parameter space containing the data points.

5 13. A method according to any one of the preceding claims wherein said data points are derived from an image, said classes corresponding to different physical parts in said image.

10 14. A method according to claim 13 wherein said property of said data points comprises a descriptor of at least part of an object in the image and the spatial coordinates of that part.

15 15. A method according to claim 14 wherein the descriptor comprises at least a value representing the shape of at least part of said object.

16. A method according to claim 15 wherein the descriptor comprises at least a value representing the size of at least part of said object.

20 17. A method according to any one of claims 13 to 16 wherein the image is a medical image.

18. A method according to any one of claims 13 to 16 wherein the image is a volumetric image or non-invasive image.

25 19. A method according to any one of claims 13 to 18 wherein the data points are taken from a spatial model fitted to said image.

30 20. A method of demarcating different parts of a structure in a representation of the structure, comprising the steps of calculating for each of a plurality of data points in the representation at least one shape descriptor of the structure at that point, and

segmenting the representation on the basis of said at least one shape descriptor.

21. A method according to claim 20 wherein the descriptor comprises values representing the cross-sectional size of the structure at that point.

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22. A method according to claim 21 wherein the values representing the cross-sectional size are the lateral dimensions of the structure at that point.

23. A method according to any one of claims 20 to 22 wherein the representation is a
10 spatial model fitted to an image of the structure.

24. A method according to any one of claims 20 to 23 wherein the representation is segmented automatically.

15 25. A method according to claim 24 wherein the representation is segmented using an unsupervised segmentation method.

26. A method according to any one of claims 20 to 23 wherein the representation is segmented by hand.

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27. A method according to any one of claims 20 to 26 wherein the structure is in the human or animal body.

28. A method according to any one of claims 20 to 26 wherein the representation is a
25 medical image.

29. A method according to any one of claims 20 to 26 wherein the image is a volumetric or non-invasive image.

30 30. A method according to any one of claims 20 to 29 wherein the representation is a

model of the structure.

31. A method according to any one of claims 20 to 30 wherein the segmentation method is in accordance with any one of claims 1 to 19.

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32. A computer program comprising program code means for executing on a programmed computer the method of any one of the preceding claims.

33. Apparatus for segmenting a data set of multi-dimensioned data points, the
10 apparatus comprising:
 means for receiving the data set;
 a data processor for segmenting the data set in accordance with the method of
any one of claims 1 to 19; and
 a display device for displaying the segmented data set.

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34. Apparatus according to claim 33 wherein the means for receiving the data set comprises an acquisition device for acquiring the data set from a subject.

35. Apparatus for demarcating different parts of a structure in a representation of the
20 structure, the apparatus comprising:
 means for receiving said representation in the form of a data set;
 a data processor for processing said data set to demarcate the different parts
of the structure in accordance with the method of any one of claims 20 to 31.

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ABSTRACT
UNSUPERVISED DATA SEGMENTATION

An unsupervised method of segmenting data sets using a region growing
5 technique in which data points are initially assigned to a single class, new classes are
seeded and points in the data set tested by calculating the probability that they belong
to the new class. The probability distributions used in the calculation are adapted as
points are reassigned. Classes which fail to grow are discarded. The technique may
be applied to the segmentation of data sets in which the data points are taken from
10 medical images. The method may be applied to the demarcation of different parts of
structures, e.g. in the medical field demarcating an aneurysm from the surrounding
blood vessels in an image or 3-D model of a patient's vasculature. The method may
involve using a shape descriptor which is representative of the shape of the structure
at each point under consideration. Thus the different parts are distinguished on the
15 basis of their shape.

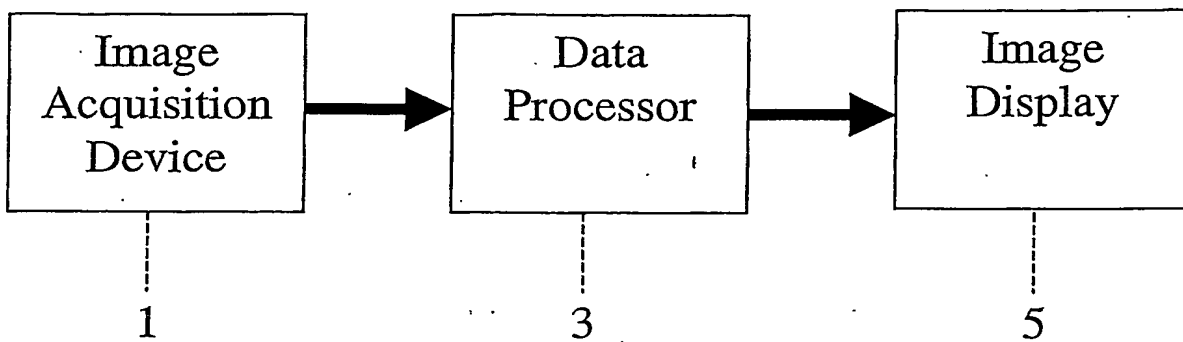


Figure 1: Schematic of imaging system.

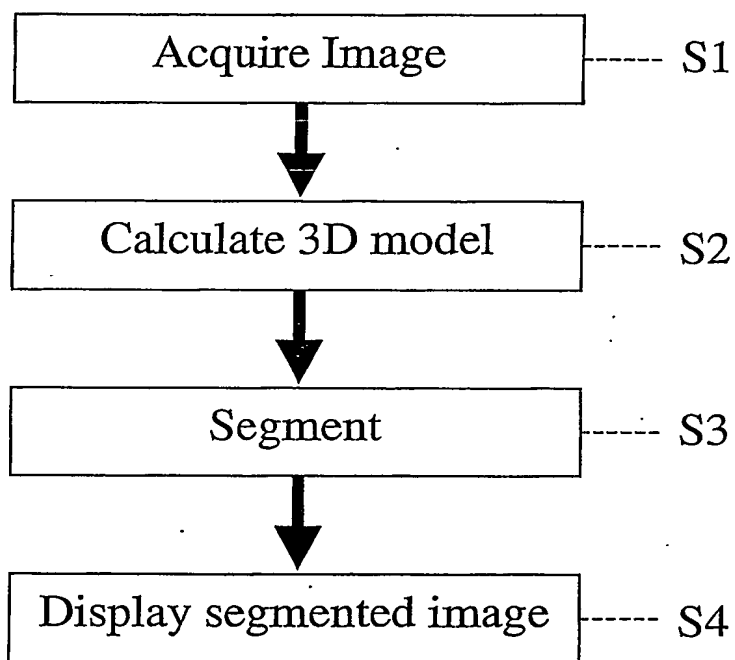


Figure 2: Flow diagram of one embodiment of the invention.

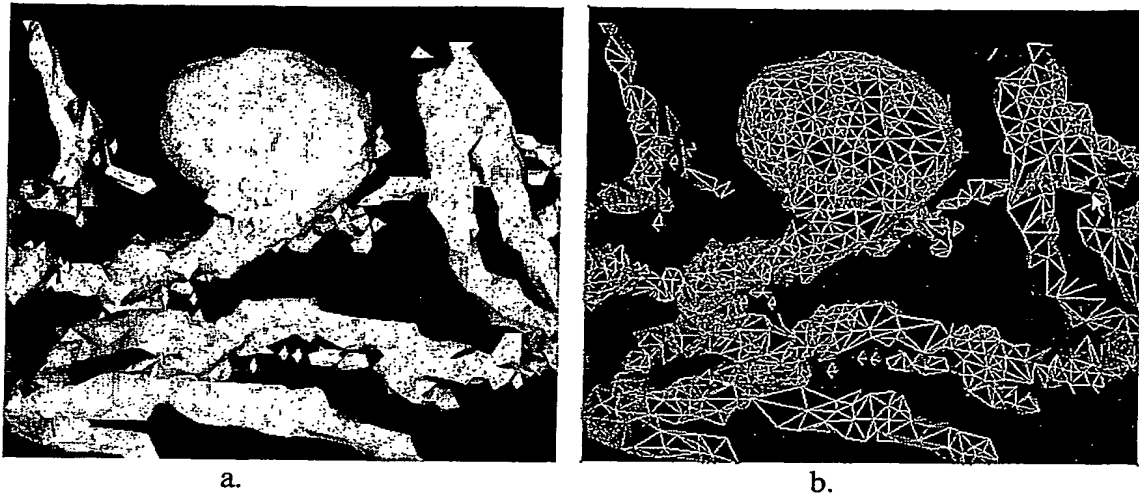


Figure 3: a.) 3-D model of an aneurysm and adjoining vessels. b.) Mesh computed for the 3-D model.

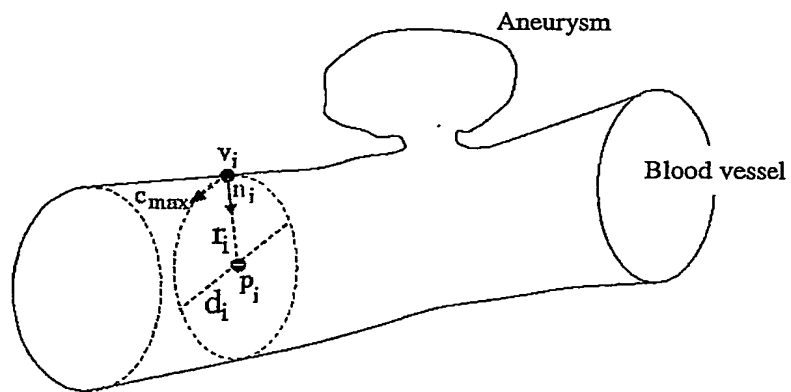


Figure 4: Local shape descriptors, vessel radius and the perpendicular diameter.

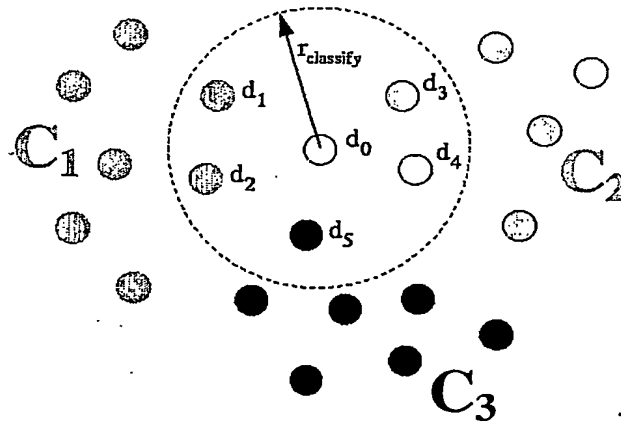


Figure 5: Point and neighbourhood.

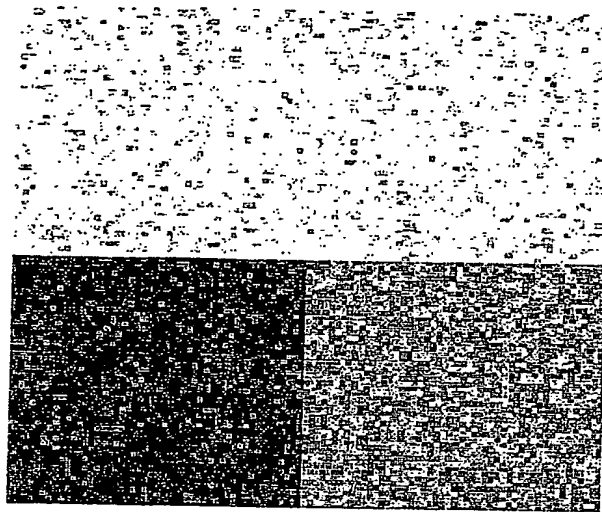


Figure 6: Synthetic data containing three groups.

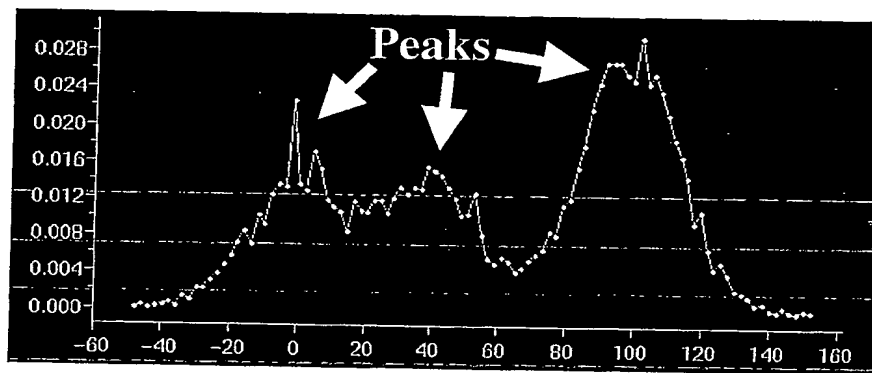


Figure 7: Initial Probability $P(v_j | d_j \in C_0)$.

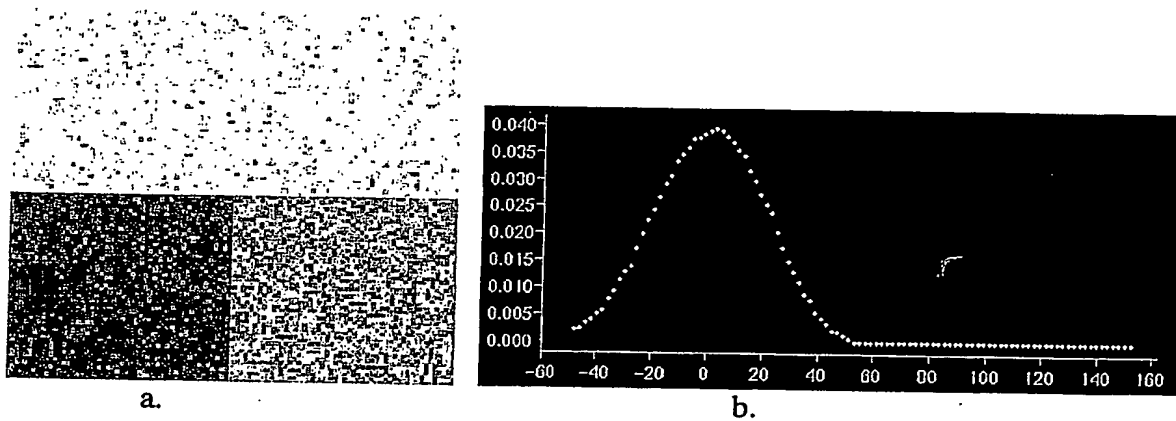


Figure 8: a.) Seed for Class C_1 . b.) Initial probability for $P(v_j | d_j \in C_1)$.

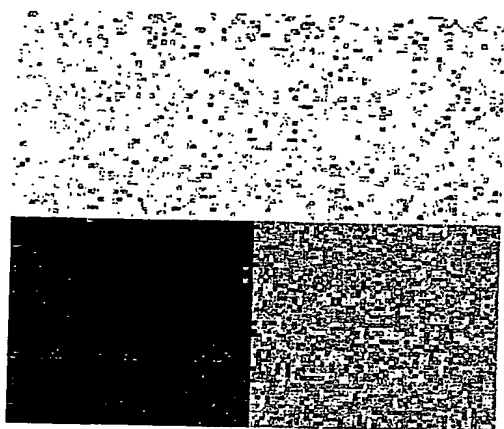


Figure 9: Classification after C_1 converges.

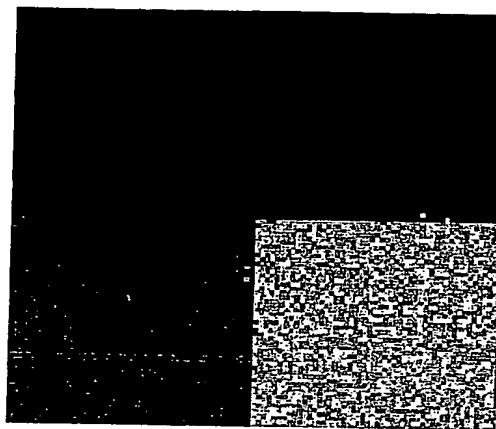
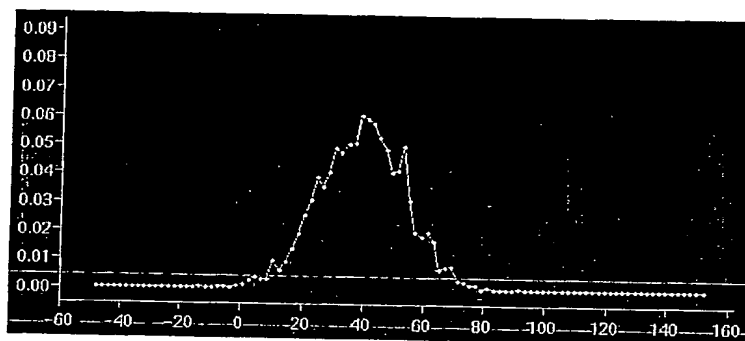
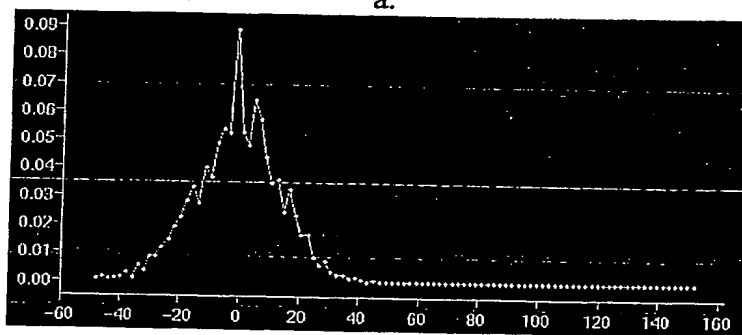


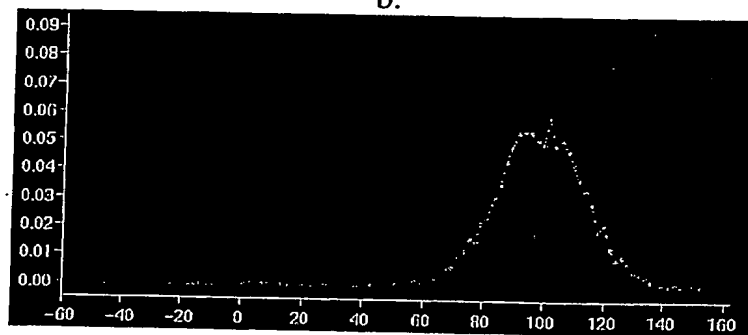
Figure 10: Classification after C_2 converges.



a.



b.



c.

Figure 11: Probability densities after C_2 converges. a.) $P(v_j | d_j \in C_0)$. b.) $P(v_j | d_j \in C_1)$. c.) $P(v_j | d_j \in C_2)$.

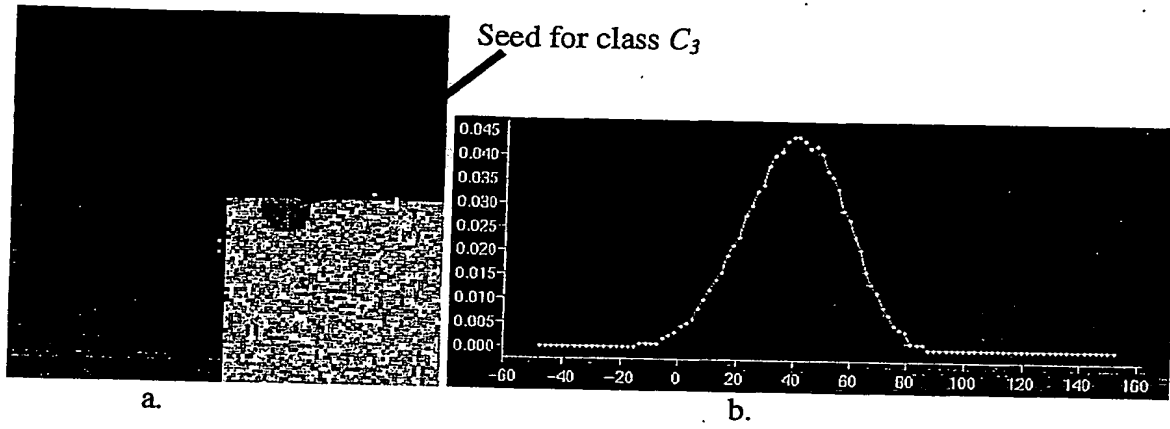


Figure 12: a.) Seed for Class C_3 . b.) Initial probability for $P(v_j | d_j \in C_3)$.

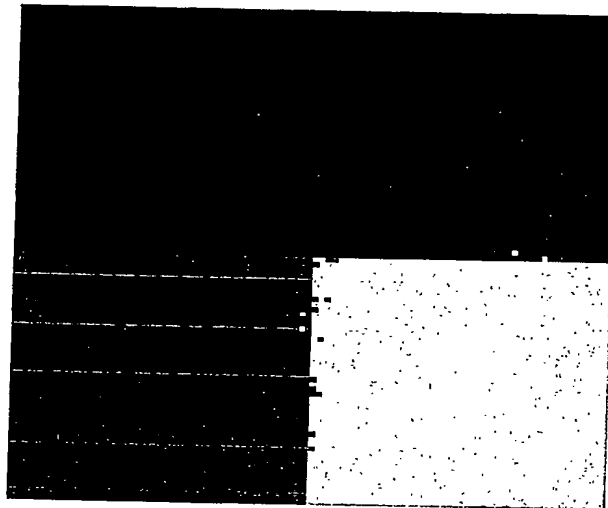


Figure 13: Final segmentation of synthetic data.

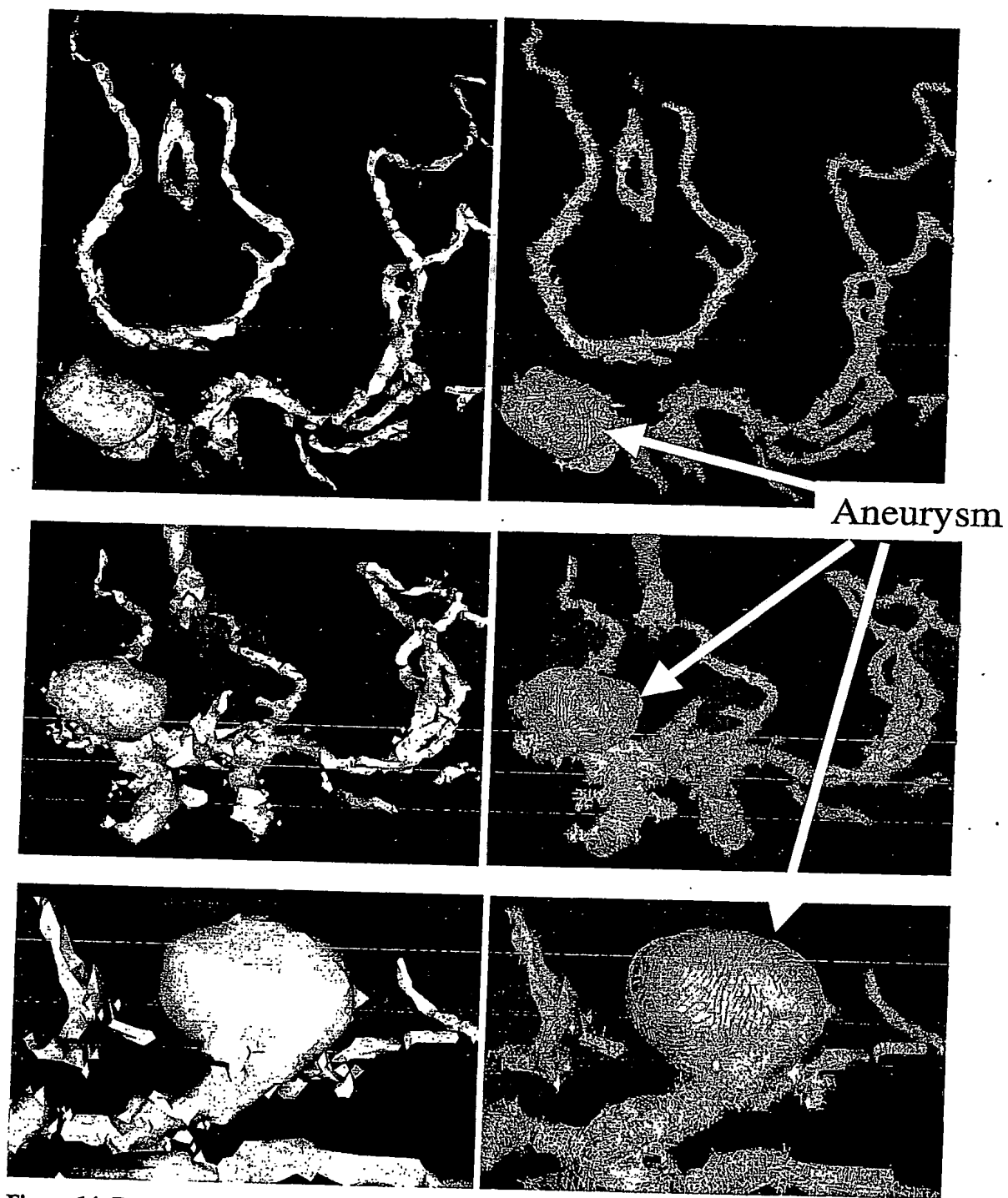


Figure 14: Results for patient 1.

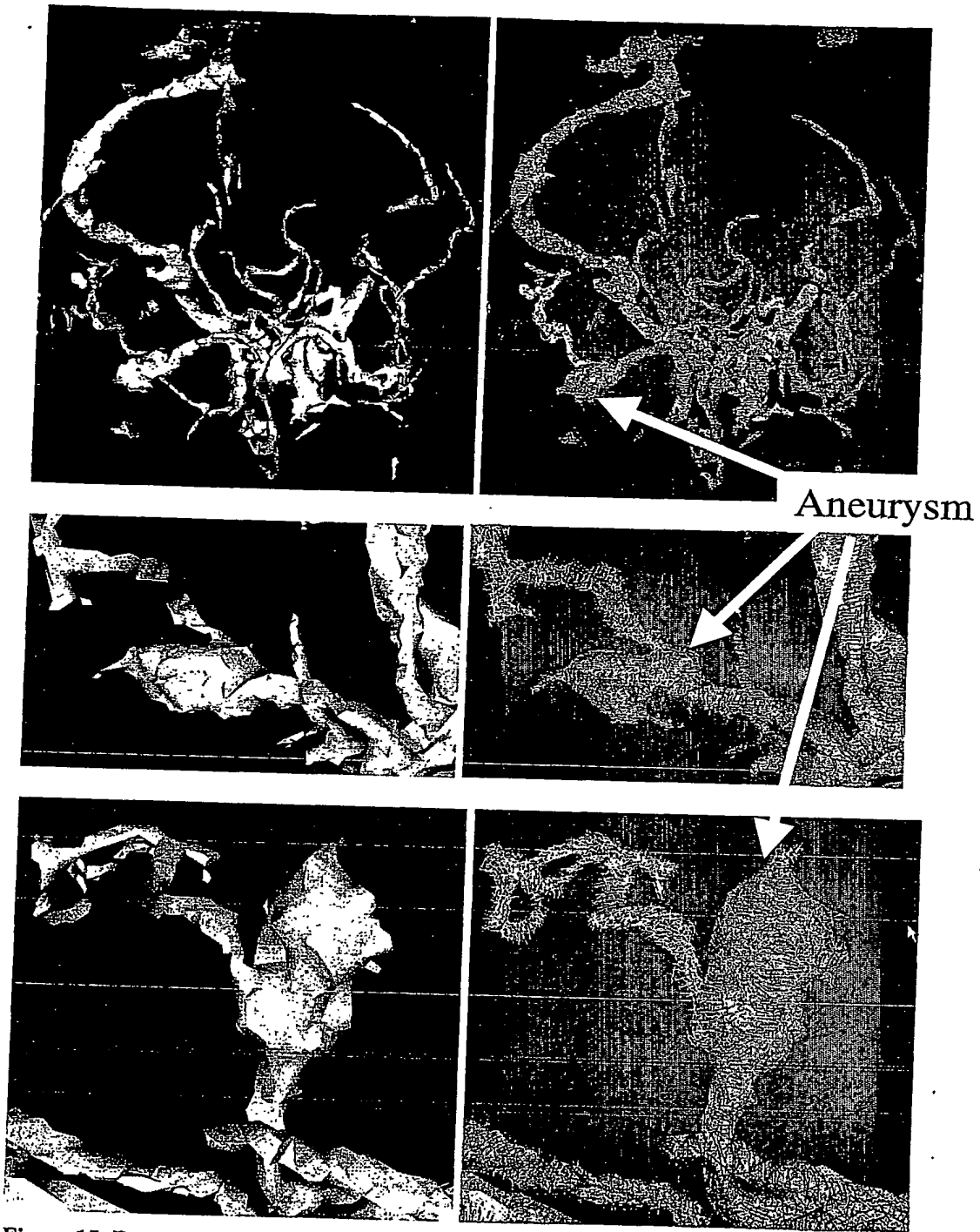


Figure 15: Results for patient 2.

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